Integral binary quadratic forms was deeply studied by Gauss, and his work led to many questions, some still open, concerning class numbers $h_D$ of quadratic fields. After an introduction to these matters, this talk will move to discuss central $L$-values of modular forms and indicate an intriguing relationship of their averages to class numbers.